

4763

Mark Scheme

June 2012

Question		Answer	Marks	Guidance
1	(iv)	$T = M^\alpha L^\beta (MLT^{-2})^\gamma$ $\gamma = -\frac{1}{2}$ $\alpha + \gamma = 0, \beta + \gamma = 0$ $\alpha = \frac{1}{2}, \beta = \frac{1}{2}$	B1 M1 A1A1 [4]	CAO Considering powers of M or L FT $\alpha = -\gamma, \beta = -\gamma$ (provided non-zero)
1	(v)	$0.718 = k(8)^{\frac{1}{2}}(0.4)^{\frac{1}{2}}(125)^{-\frac{1}{2}}$ $k = 4.4875$ $t = (4.4875)(75)^{\frac{1}{2}}(3)^{\frac{1}{2}}(20)^{-\frac{1}{2}}$ New time is 15.1 s (3 sf)	M1 M1 A1 [3]	Obtaining equation for k Obtaining expression for new time CAO <i>No penalty for using $b = 1.2$ and $b = 9$</i> Or using ratio and powers Or $\times \left(\frac{75}{8}\right)^{\frac{1}{2}} \times \left(\frac{3}{0.4}\right)^{\frac{1}{2}} \times \left(\frac{20}{125}\right)^{-\frac{1}{2}}$
2	(a)	(i) $R \cos 18^\circ = 800 \times 9.8 \quad (R = 8243)$ $R \sin 18^\circ = 800 \times \frac{v^2}{45}$ $\tan 18^\circ = \frac{v^2}{45 \times 9.8}$ Speed is 12.0 ms^{-1} (3 sf)	M1 M1 A1 A1 [4]	Resolving vertically Horizontal equation of motion Might also include F Might also include F
2	(a)	(ii) $R \cos 18^\circ = F \sin 18^\circ + 800 \times 9.8$ $R \sin 18^\circ + F \cos 18^\circ = 800 \times \frac{15^2}{45}$ Frictional force is 1380 N (3 sf) Normal reaction is 8690 N (3 sf)	M1 A1 M1 A1 M1 A1 A1 [7]	Resolving vertically (three terms) Horizontal equation (three terms) Obtaining a value for F or R <i>Dependent on previous M1M1</i>

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2	(b)	$\frac{1}{2}m(7^2 - 2.8^2) = mg(a + a \cos \theta)$ $a(1 + \cos \theta) = 2.1$ $mg \cos \theta = m \times \frac{2.8^2}{a}$ $a \cos \theta = 0.8$ <p>Length of string is 1.3 m Angle with upward vertical is 52.0° (3 sf)</p>	M1 A1 M1 A1 M1 A1 A1 [7]	Equation involving KE and PE Correct equation involving a and θ Radial equation of motion Correct equation involving a and θ Eliminating θ or a Dependent on previous M1M1 A0 for 128° or 38° $h = 2.1$ implies M1 a is length of the string (Might use angle with downward vertical or horizontal) Might also involve T
3	(i)	$\dot{x} = -A\omega \sin(\omega t - \phi)$ $\ddot{x} = -A\omega^2 \cos(\omega t - \phi)$ $\ddot{x} = -\omega^2(x - c)$	B1 M1 E1 [3]	Obtaining second derivative Correctly shown Allow one error
3	(ii)	$c = 10$ $A = 6$ $\frac{2\pi}{\omega} = 10$ $\omega = \frac{\pi}{5}$ $x = 16 \text{ when } t = 3 \Rightarrow 3\omega - \phi = 0$ $\phi = \frac{3\pi}{5}$	B1 B1 M1 A1 M1 A1 [6]	Accept $A = -6$ Using $\frac{2\pi}{\omega}$ Accept $\omega = -\frac{\pi}{5}$ Obtaining simple relationship between ϕ and ω . NB $\phi = 3$ is M0 NB other values possible If exact values not seen, give A0A1 for both $\omega = 0.63$ and $\phi = 1.9$ Max 5/6 if values are not consistent Or other complete method for finding ω Allow $\frac{2\pi}{10}$ etc Or $x = 10 + 6 \cos\left\{\frac{\pi}{5}(t - 3)\right\}$ e.g. $\phi = -\frac{7\pi}{5}$, $\phi = \frac{13\pi}{5}$, $x = 10 - 6 \cos\left(\frac{\pi}{5}t - \frac{8\pi}{5}\right)$ etc

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3	(iii)	Maximum speed is $A\omega$ Maximum speed is $\frac{6\pi}{5}$ or 3.77 ms^{-1} (3 sf)	M1 A1 [2]	Or e.g. evaluating \dot{x} when $t = 5.5$ FT is $ A\omega $ (must be positive)	
3	(iv)	When $t = 0$, height is 8.15 m (3 sf) $v = -\frac{6\pi}{5} \sin\left(\frac{\pi t}{5} - \frac{3\pi}{5}\right)$ When $t = 0$, velocity is 3.59 ms^{-1} (3 sf)	B1 M1 A1 [3]	FT is $c + A\cos\phi$ (provided $4 < x < 16$) Or $v^2 = \left(\frac{\pi}{5}\right)^2 (6^2 - 1.854^2)$ FT is $A\omega\sin\phi$ (must be positive)	Must use radians <i>Allow one error in differentiation</i> ($\phi = 3$ gives $x = 4.06$, $v = 0.532$)
3	(v)	When $t = 0$, $x = 8.146$ When $t = 14$, $x = 14.854$ $(16 - 8.146) + 12 + 12 + (16 - 14.854)$ Distance is 33 m	M1 M1 M1 A1 [4]	Finding x when $t = 14$ ($16 - 14.854$) used Fully correct strategy CAO	Correct (FT) value, or evidence of substitution, required ($\phi = 3$ gives $x = 15.3$) Requires $4 < x(14) < 16$ Also requires $4 < x(0) < 16$

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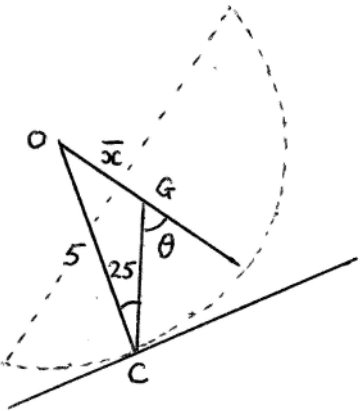
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4 (a)	$A = \int_0^9 (3 - \sqrt{x}) dx$ $= \left[3x - \frac{2}{3}x^{\frac{3}{2}} \right]_0^9 \quad (=9)$ $A\bar{x} = \int xy dx = \int_0^9 x(3 - \sqrt{x}) dx$ $= \left[\frac{3}{2}x^2 - \frac{2}{5}x^{\frac{5}{2}} \right]_0^9 \quad (=24.3)$ $\bar{x} = \frac{24.3}{9} = 2.7$ $A\bar{y} = \int \frac{1}{2}y^2 dx = \int_0^9 \frac{1}{2}(3 - \sqrt{x})^2 dx$ $= \left[\frac{9}{2}x - 2x^{\frac{3}{2}} + \frac{1}{4}x^2 \right]_0^9 \quad (=6.75)$ $\bar{y} = \frac{6.75}{9} = 0.75$	<p>M1</p> <p>A1</p> <p>M1</p> <p>A1</p> <p>A1</p> <p>M1</p> <p>M1</p> <p>A1</p> <p>A1</p> <p>[9]</p>	<p>For $3x - \frac{2}{3}x^{\frac{3}{2}}$</p> <p>For $\int xy dx$</p> <p>For $\frac{3}{2}x^2 - \frac{2}{5}x^{\frac{5}{2}}$</p> <p>For $\int \dots y^2 dx$</p> <p>Expanding (three terms) and integrating (allow one error)</p> <p>For $\frac{9}{2}x - 2x^{\frac{3}{2}} + \frac{1}{4}x^2$</p> <p>Or $\int_{(0)}^{(3)} (3-y)^2 y dy$</p> <p>Or $\frac{9}{2}y^2 - 2y^3 + \frac{1}{4}y^4$</p>

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4	(b)	(i)	$V = \int_2^5 \pi(25 - x^2) dx$ $= \pi \left[25x - \frac{1}{3}x^3 \right]_2^5 \quad (= 36\pi)$ $V\bar{x} = \int \pi xy^2 dx = \int_2^5 \pi x(25 - x^2) dx$ $= \pi \left[\frac{25}{2}x^2 - \frac{1}{4}x^4 \right]_2^5 \quad (= \frac{441\pi}{4})$ $\bar{x} = \frac{\frac{441}{4}\pi}{36\pi} = \frac{49}{16} \quad (= 3.0625)$	M1 A1 M1 A1 A1 [5]	For $\int \dots (25 - x^2) dx$ For $25x - \frac{1}{3}x^3$ For $\int xy^2 dx$ For $\frac{25}{2}x^2 - \frac{1}{4}x^4$ Accept 3.1 from correct working
4	(b)	(ii)	 $\frac{\sin \theta}{5} = \frac{\sin 25^\circ}{\bar{x}}$ $\theta = 43.6^\circ$	M1 M1 M1 A1 [4]	Lenient, if CG drawn. Needs to be quite accurate if CG not drawn CG is vertical (<i>may be implied</i>) Using triangle OGC <i>or equivalent</i> Accept art 43° or 44° from correct work FT is $\sin^{-1}\left(\frac{2.113}{\bar{x}}\right)$ Provided $2.113 < \bar{x} < 5$